

Klaus Hermann

Crystallography and Surface Structure

An Introduction for Surface Scientists and Nanoscientists

Second, Revised and Expanded Edition

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