

REVIEWS in MINERALOGY Volume 32

*STRUCTURE, DYNAMICS
AND PROPERTIES OF
SILICATE MELTS*

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Front cover: Sketch of a possible mechanism for the exchange of silicon species. Oxygens: open circles; network-modifying cations: cross-hatched circles; silicons: solid circles. From Farnan and Stebbins (1994; see Fig. 17, p. 222)

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STRUCTURE, DYNAMICS AND PROPERTIES OF SILICATE MELTS

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