

Computer Simulations of Molecules and Condensed Matter

From Electronic Structures
to Molecular Dynamics

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