

Nonlinear Dynamics of  
Poly(hydroxyalkanoate) Production  
in *Ralstonia eutropha*  
and *Rhodospirillum rubrum*

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