

Statistical analysis of stress and deformation state in polycrystalline aggregates with a large number of grains

Dissertation

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