

Lessons from Nanoscience:
A Lecture Note Series

Vol. **2**

NEAR-EQUILIBRIUM TRANSPORT

Fundamentals and Applications

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Contents

<i>Preface</i>	vii
<i>Acknowledgments</i>	ix
<i>List of Figures</i>	xv
1. Overview	1
1.1 Introduction	1
1.2 Diffusive electron transport	2
1.3 Types of electron transport	4
1.4 Why study near-equilibrium transport?	6
1.5 About these lectures	6
1.6 Summary	9
1.7 References	9
2. General Model for Transport	13
2.1 Introduction	13
2.2 Mathematical model	15
2.3 Modes	18
2.4 Transmission	23
2.5 Near-equilibrium (linear) transport	26
2.6 Transport in the bulk	27
2.7 Summary	31
2.8 References	31
3. Resistance: Ballistic to Diffusive	33
3.1 Introduction	33

3.2	2D resistors: ballistic	35
3.3	2D resistors: diffusive to ballistic	41
3.4	Discussion	44
3.5	Summary	55
3.6	References	56
4.	Thermoelectric Effects: Physical Approach	59
4.1	Introduction	59
4.2	Electric current flow: Seebeck effect	61
4.3	Heat current flow: Peltier effect	66
4.4	Coupled flows	70
4.5	Thermoelectric devices	73
4.6	Discussion	77
4.7	Summary	80
4.8	References	81
5.	Thermoelectric Effects: Mathematics	83
5.1	Introduction	83
5.2	Driving forces for current flow	84
5.3	Charge current	85
5.4	Heat current	87
5.5	Discussion	89
5.6	Summary	102
5.7	References	102
6.	An Introduction to Scattering	105
6.1	Introduction	105
6.2	Physics of carrier scattering	106
6.3	Transmission and mean-free-path	110
6.4	Mean-free-path and scattering	112
6.5	Discussion	114
6.6	Summary	120
6.7	References	120
7.	Boltzmann Transport Equation	123
7.1	Introduction	123
7.2	The Boltzmann Transport Equation	124
7.3	Solving the steady-state BTE	127

7.4	Transport coefficients	129
7.5	Magnetic fields	134
7.6	Discussion	140
7.7	Summary	141
7.8	References	142
8.	Near-equilibrium Transport: Measurements	143
8.1	Introduction	143
8.2	Resistivity/conductivity measurements	146
8.3	Hall effect measurements	148
8.4	The van der Pauw method	151
8.5	Temperature-dependent measurements	155
8.6	Discussion	158
8.7	Summary	165
8.8	References	165
9.	Phonon Transport	169
9.1	Introduction	169
9.2	Electrons and phonons	170
9.3	General model for heat conduction	175
9.4	Thermal conductivity	178
9.5	Debye model for $M_{\text{ph}}(\hbar\omega)$	182
9.6	Phonon scattering	184
9.7	Discussion	187
9.8	Summary	189
9.9	References	190
10.	Graphene: A Case Study	193
10.1	Introduction	193
10.2	Graphene	194
10.3	Density-of-states and carrier density	197
10.4	Number of modes and conductance	198
10.5	Scattering	199
10.6	Conductance vs. carrier density	202
10.7	Discussion	205
10.8	Summary	209
10.9	References	209
	Appendix A Summary of Key Results	211
	<i>Index</i>	223