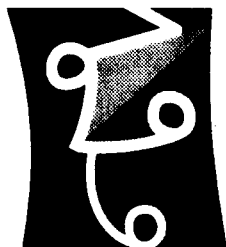


International Group for the Psychology of
Mathematics Education



PME 20

**Proceedings of the 20th Conference of the
International Group for the Psychology of
Mathematics Education**

Edited by

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Volume 1

Valencia (Spain), July 8 - 12, 1996

Universitat de València
Dept. de Didàctica de la Matemàtica

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