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Harmonic Analysis
in Operator Algebras
and its Applications to Index
Theory and Topological
Solid State Systems

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