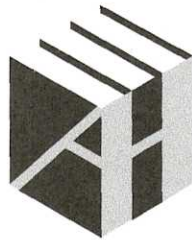


The Fiber-Optic Gyroscope

Third Edition

Hervé C. Lefèvre



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