

# **Resource-Constrained Wireless Sensory Agents: Localization, Tracking and Environment Mapping**

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