

Simulation of Thermo-Chemo-Mechanical Coupled Additive Manufacturing Processes using Peridynamics

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