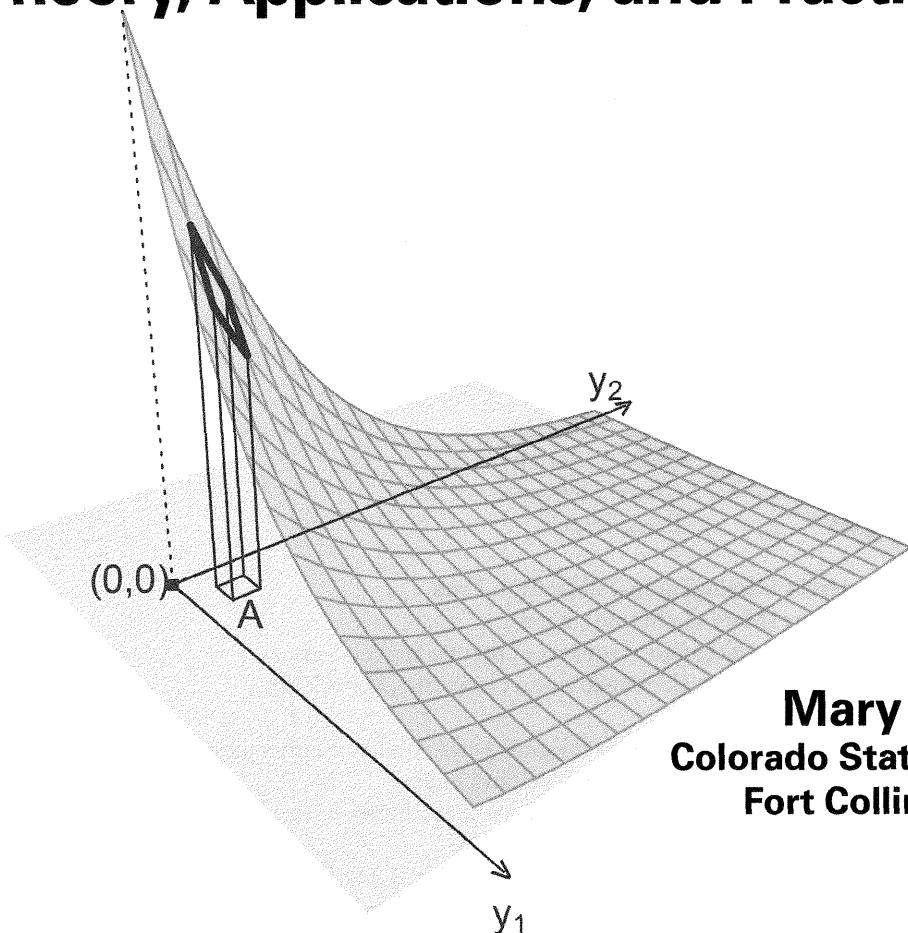


Probability and Mathematical Statistics

Theory, Applications, and Practice in R



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