

# Micro and Macro Mechanical Assessment of Small and Intermediate Strain Properties of Granular Material

Dissertation

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