

Dirichlet's principle

a mathematical comedy of errors
and its influence on the development
of analysis

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