

DISCRETE MATHEMATICS AND ITS APPLICATIONS
Series Editor KENNETH H. ROSEN

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**GRAPH ALGORITHMS
AND OPTIMIZATION**

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