

# COOPERATIVE GAME THEORY AND APPLICATIONS

*Cooperative Games Arising from  
Combinatorial Optimization Problems*

*by*

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