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# Capillarity and Wetting Phenomena

Drops, Bubbles, Pearls, Waves

Translated by Axel Reisinger

With 177 Figures



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