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Dramatis personae

David	David Hilbert (1862–1943)
Emil	Emil Post (1897–1954)
Kurt	Kurt Gödel (1906–1978)
Tarzan	A traveller
Bolgani	A guide

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