

Developments in Geotechnical Engineering, 85

Fundamentals of Discrete Element Methods for Rock Engineering

Theory and Applications

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