

# The Future of Theoretical Physics and Cosmology

Celebrating Stephen Hawking's 60th Birthday

Edited by

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