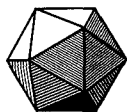


The Dolciani Mathematical Expositions

NUMBER SEVENTEEN

From Erdős to Kiev
Problems of Olympiad Caliber

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Contents

Preface	xi
Seven Solutions by George Evagelopoulos	1
A Decomposition of a Triangle	13
AIME—1987	19
A Problem from the 1991 AIME Examination	25
Nine Unused Problems from the 1987 International Olympiad	29
Two Problems from the 1988 USA Olympiad	55
From the 1988 International Olympiad	59
A Geometric Gem of Duane DeTemple	63
A Kiev Olympiad Problem	67
Some Student Favorites	71
Four Unused Problems from the 1988 International Olympiad	79
From the 1988 AIME Examination	93
An Unused Bulgarian Problem on the Medial Triangle and the Gergonne Triangle	99
Two Solutions by John Morvay from the 1982 Leningrad High School Olympiad	103
Two Solutions by Ed Doolittle	107
From the 1987 Spanish Olympiad	115
A Problem from Johann Walter	119
From the 1987 Balkan Olympiad	123
From Various Kürschák Competitions	127
Two Questions from the 1986 National Junior High School Mathematics Competition of the People's Republic of China	141
	ix

From the 1986 Spanish Olympiad	145
A Geometric Construction	147
An Inequality Involving Logarithms	151
On Isosceles Right-Angled Pedal Triangles	153
Two Problems from the 1987 Austrian Olympiad	159
From the 1988 Canadian Olympiad	167
A Problem on Closed Sets	171
From the 1987 Austrian-Polish Team Competition	173
Two Problems from the 1987 Austrian-Polish Mathematics Competition	177
An Engaging Property Concerning the Incircle of a Triangle	183
On Floors and Ceilings	187
Two Problems from the 1987 International Olympiad	191
On Arithmetic Progressions	197
A Property of Triangles Having an Angle of 30°	199
From the 1985 Bulgarian Spring Competition	203
An Unused International Olympiad Problem from Britain	207
A Rumanian Olympiad Proposal	209
From the 1984 Bulgarian Olympiad	211
Two Erdős Problems	213
From the 1985 Bulgarian Olympiad	217
From a Chinese Contest	221
A Japanese Temple Geometry Problem	223
Two Problems from the Second Balkan Olympiad, 1985	229
A Property of Pedal Triangles	235
Three More Solutions by George Evagelopoulos	239
The Power Mean Inequality	249