Four Essays on
the Empirical Properties of Stock Market Volatility

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\(^1\) This chapter is identical to the article that has been published in European Financial Management: Masset, P. / Wallmeier, M. (2010), A high-frequency investigation of the interaction between volatility and DAX returns, European Financial Management 16(3), pp. 327-344.
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