Counterparty Credit Risk and Credit Value Adjustment

A Continuing Challenge for Global Financial Markets

Second Edition

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