Léon Walras
ELEMENTS OF
PURE ECONOMICS
OR
THE THEORY OF SOCIAL WEALTH

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PART I
Object and Divisions of
Political and Social Economy

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ADAM SMITH; J. B. SAY

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**PART III**

Theory of Exchange of Several Commodities for One Another

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