STOCHASTIC DOMINANCE
IN PORTFOLIO ANALYSIS AND ASSET PRICING

Stochastische dominatie in portefeuilleanalyse en de prijsvorming van effecten

Thesis

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Contents

1 Introduction 1

2 SD Efficiency Analysis of Diversified Portfolios: Classification, Comparison and Refinements 5
   2.1 Introduction .................................................. 6
   2.2 Unified framework .......................................... 9
   2.3 Second Order (SSD) Efficiency ............................ 14
      2.3.1 Revealed Preference Approach ........................ 15
      2.3.2 Majorization Approach ................................. 17
      2.3.3 Distribution-Based Approach .......................... 21
   2.4 Extensions .................................................. 26
      2.4.1 FSD Efficiency and Optimality ........................ 26
      2.4.2 Unrestricted shortsales ................................. 27
   2.5 Comparison of SSD methods ................................. 29
   2.6 Concluding remarks ........................................ 31

3 Stochastic Dominance: Convexity and Some Efficiency Tests 33
   3.1 Introduction ................................................ 33
   3.2 Problem formulation and assumptions ...................... 35
   3.3 Convexity .................................................. 37
      3.3.1 Homogeneous preferences .............................. 40
   3.4 Generalizing preferences: non-convexity and some efficiency tests ........................................... 42
      3.4.1 SSD Efficiency ....................................... 44
      3.4.2 TSD Efficiency ....................................... 47
<table>
<thead>
<tr>
<th>3.4.3</th>
<th>Stochastic Dominance for Decreasing Absolute Risk Aversion (DSD)</th>
<th>48</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.4.4</td>
<td>SD for Decreasing Absolute and Increasing Relative Risk Aversion (DISD)</td>
<td>51</td>
</tr>
<tr>
<td>3.5</td>
<td>Concluding remarks</td>
<td>52</td>
</tr>
</tbody>
</table>

4 Tractable Almost Stochastic Dominance 57
4.1 Introduction .................................................. 57
4.2 Almost Stochastic Dominance ................................... 61
4.3 Linear Programming Models for $\varepsilon$-ASSD ............. 67
4.4 Application: Stocks in the long run .......................... 69
4.5 Concluding remarks .............................................. 78

5 Stochastic Dominance and Full- and Partial Moments in Dynamic Asset Allocation. 81
5.1 Introduction ...................................................... 81
5.2 Data and Methodology ............................................ 83
   5.2.1 Full vs. partial moments: MV-, LPM- and SDV-efficient portfolios. ........................................ 84
   5.2.2 Second Order Stochastic Dominance (SSD) strategy. .... 86
   5.2.3 Other strategies considered. ............................. 88
5.3 Realized performance. ............................................ 90
   5.3.1 Realized return ............................................. 90
   5.3.2 Realized risk. ............................................... 92
5.4 Robustness check: Bootstrapping. ............................... 96
5.5 Concluding remarks .............................................. 97

6 Conclusions and suggestions for further research 103
   Robust Stochastic Dominance .................................... 105

Samenvatting (Summary in Dutch) 109

Bibliography 111