

Derivatives and the Asset Allocation Decision: a Synthesis between Portfolio Diversification and Portfolio Insurance

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