KARL-EUGEN KURRER

The History of the Theory of Structures
From Arch Analysis to Computational Mechanics
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