Physics of Transitional Shear Flows

Instability and Laminar–Turbulent Transition in Incompressible Near-Wall Shear Layers

Springer
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