A Framework for Modeling the Mechanical Behavior of Tempered Martensitic Steels at High Temperatures

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zur Erlangung des akademischen Grades

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