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**Discrete Element based numerical simulation  
of crack formation in brittle material by  
swelling cement**

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