Mechanics and Physics of Energy Density

Characterization of material/structure behavior with and without damage

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