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Selected Works of A. N. Kolmogorov

Volume III Information Theory and the Theory of Algorithms

edited by

A. N. Shirayev

Translated from the Russian by A. B. Sossinsky



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