

# Transmission Strategies for Broadband Wireless Systems with MMSE Turbo Equalization

Marcus Großmann



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1. Gutachter: Prof. Dr.-Ing. habil. Reiner Thomä  
(Technische Universität Ilmenau)

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(Universität Rostock)

3. Gutachter: Dr.-Ing. Werner Teich  
(Universität Ulm)

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