Introduction to Practice of Molecular Simulation
Molecular Dynamics, Monte Carlo, Brownian Dynamics, Lattice Boltzmann, Dissipative Particle Dynamics

Akira Satoh
Akita Prefectural University
Japan
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