Electromagnetic Field Interaction with Transmission Lines

From classical theory to HF radiation effects

Edited by

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PART I: CLASSICAL TRANSMISSION LINE THEORY

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