

**A First-Principles Statistical Mechanics
Study of the Ordering Behavior of
Hydrogen on Pd(111) at Low
Temperatures**

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