Plasma Physics
Basic Theory with Fusion Applications

Third, Revised Edition
With 80 Figures

Springer
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