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Electron Diffraction and High-Resolution Electron Microscopy of Mineral Structures

With 126 Figures

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