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Nonclassical Thermoelastic Problems in Nonlinear Dynamics of Shells

Applications of the Bubnov-Galerkin and Finite Difference Numerical Methods

With 222 Figures

Springer
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