Quasielastic Neutron Scattering

Principles and Applications in Solid State Chemistry, Biology and Materials Science

M Bée

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