NONLINEAR GRAVITODYNAMICS
The Lense-Thirring Effect
A documentary introduction to current research

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