Boundary Value Problems and Symplectic Algebra for Ordinary Differential and Quasi-Differential Operators

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