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Classical Mathematical Physics

Dynamical Systems
and Field Theories

Third Edition

Translated by Evans M. Harrell II

With 146 Illustrations



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