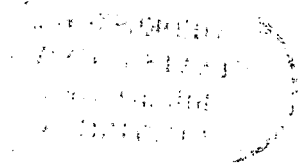


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Poincaré and the Three Body Problem

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